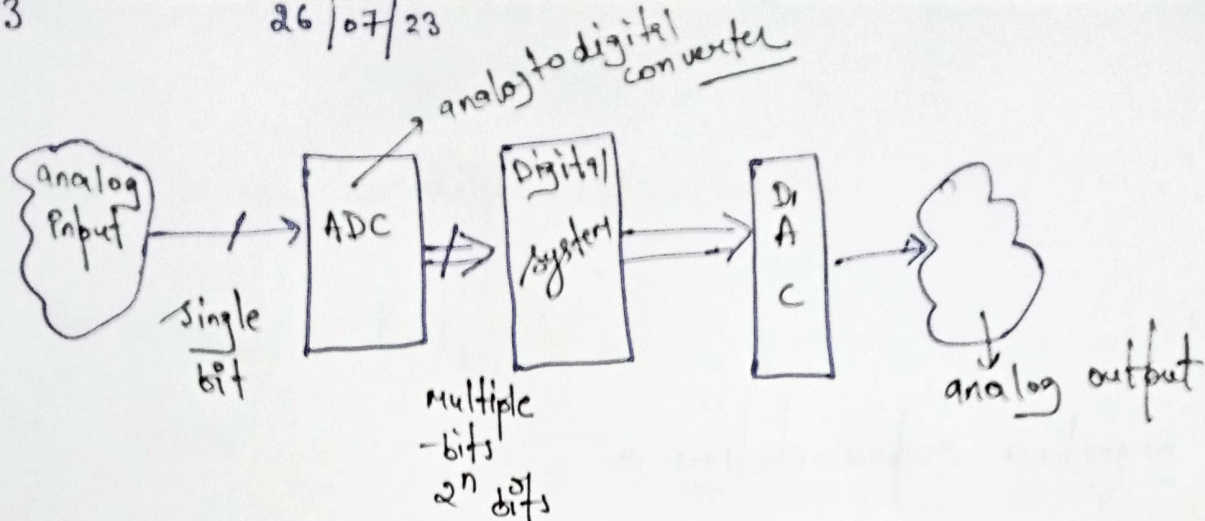


26/07/23



Digital system →

Computer, Calculator, Digital clock,
Digital voltmeter (measurement instrument)

How complex is a system going to be depends on application.

e.g. take recent processor (speed is in GHz and ckt complexity is enormous and for washing machine (controller inside) is less.

Basic Building Block of computer →

cpu, memory

input, output unit

cpu → ALU → ADD, sub, multiplier
(Arithmetic)
↓
logic, control unit

system → subsystem → modules

Number representation →

Assumptions

1. we work with voltage (0 to 5V)

0' → 0V switch off

1' → 5V switch on

for 3 switch, $2^3 = 8$ level.

for $n=2$, $= 2^2 = 4$

00 → off off

01 → off on

10 → on off

11 → on on

to ↑ accuracy ↑ no. of switch.

Digital electronics

conversion a no. in diff base number.

Ex

$$(45.625)_{10} = (?)_2 = (?)_x$$

$\swarrow$ $\downarrow$
 45 0.625

$x \rightarrow 2$

45	→ 1
22	→ 0
11	→ 1
5	→ 1
2	→ 0
1	→ 1

$$0.625 \times x_2 = 1.250$$

$$1 \leftarrow 1.250$$

$$0.250 \times 2$$

$$0 \leftarrow 0.500$$

$$0.500 \times 2 \rightarrow (0.625)_{10}$$

$$1 \leftarrow 1.00$$

$$= (0.101)_2$$

$$(45)_{10} = (101101)_2 = (231)_4$$

Now

$$(45.625) = (101101.101)_2$$

Binary to decimal system →

$$(101101.101)_2 = (?)_{10}$$

$$1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 + 1 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3}$$

$$32 + 8 + 4 + 1 + 0.5 + 0.125$$

$$(45.625)_{10}$$

eg. $(231.22)_4 = (?)_{10}$

Binary

$$(101101.1010)_2$$

or

$$2 \times 4^2 + 3 \times 4^1 + 1 \times 4^0 + 2 \times 4^{-1} + 2 \times 4^{-2}$$

$$32 + 12 + 1 + \frac{2}{4} + \frac{2}{16}$$

$$= 45.625$$

eg

$$(45)_{10} = (101101)_x$$

$x = \text{Base} \rightarrow \text{always +ve integer.}$

$$45 = x^5 + x^3 + x^2 + 1$$

Representation of Number $\rightarrow$

$\Rightarrow$ unsigned number $\text{eg. } +8 = 8 = 1000.$

$\Rightarrow$ signed number $\rightarrow$ used in digit system (micro processor or)

eg. $+8 = \overset{+ve}{\boxed{0}}1000$

$-8 = \underset{-ve}{\boxed{1}}1000$

sign no. for rep. karne k liye extra bit ki jarurat hogi.

three method to rep signed number.

1) signed magnitude form

2) 1's complement form

3) 2's complement form

$\rightarrow$ (2-1)'s comp. for binary.

(base 2) $\rightarrow$ 1's comp. for decimal

10's comp

decimal

unsigned

signed

$+0 \leftarrow 00$

$+1 \leftarrow 01$

$+2 \leftarrow 10$

$+3 \leftarrow 11$

$00 \rightarrow +0$

$01 \rightarrow +1$

$10 \rightarrow -0$

$11 \rightarrow -1$

$\downarrow$
first digit $\rightarrow$ sign. neg.

1. signed magnitude form →

eg. $+4 = \begin{array}{c} 0 \ 100 \\ \downarrow \quad \downarrow \\ \text{sign} \quad \text{mag.} \end{array}$ & $-4 = \begin{array}{c} 1 \ 100 \\ \downarrow \quad \downarrow \\ \text{sign} \quad \text{mag.} \end{array}$

sign. mag. form

$\begin{array}{c} 0 \ 101 \\ \downarrow \quad \downarrow \\ + \quad \text{mag.} \end{array} = +5$ & $1 \ 101 = -5.$

4 bit
 in 8 bit.
 4 bit to 8 bit

$+5 = \begin{array}{c} 0 \ 0000 \ 101 \\ \downarrow \quad \downarrow \\ \text{sign} \quad \text{mag.} \end{array}$ & $-5 = \begin{array}{c} 1 \ 0000 \ 101 \\ \downarrow \quad \downarrow \\ \text{sign} \quad \text{mag.} \end{array}$

Range of number →

$n=2$ bit → 4 binary possible

Binary	Decimal
0 0	+0
0 1	+1
1 0	-0
1 1	+1

Range -1 to 1

$= (-1, -0, +0, +1)$

for n bit = $\frac{-(2^{n-1}-1) \text{ to } +(2^{n-1}-1)}{\text{Range.}}$

for $n=3$ bit.

Range -3 to +3

$= -3, -2, -1, -0, +0, +1, +2, +3.$

but for unsigned
 0 to +7.

so always we should use
 signed rep.

Q. To rep. -4 in signed form how much bit require. 6.

$$n=4 \quad \text{range} = -7 \text{ to } +7$$

$$n=5 \quad \text{range} = -15 \text{ to } +15$$

to rep. -4 by signed mag. form, minimum 4-bit is required.

$$\begin{array}{rcl} -4 & = & 1100 \quad = \quad 10000100 \\ & & \text{4 bit} \quad \quad \quad \text{8 bit.} \end{array}$$

Disadvantage $\rightarrow$

1. Two different representation of zero $+0, -0$.
2. Calculation is not easy.

eg.

$$x = 1100 = -4 \quad \text{min. bit} = 4$$

$$0011 = +3 \quad \text{min. bit} = 3$$

$$\begin{array}{r} 1111 \\ \hline 1111 \\ \hline \downarrow \\ -7 \end{array} \quad \begin{array}{r} 1 \\ \hline 1 \\ \hline 1001 = 11 = 101 \end{array}$$

-7 wrong ans.

now to solve

$$\begin{array}{rcl} x = -4 & = & 1100 \\ + y = -5 & = & 1101 \\ \hline & = & 11001 \\ & \downarrow & \\ & \text{min.} & \\ & 5 \text{ bit} & \\ & \text{is req.} & \end{array}$$

2). $(2^n - 1)$'s or 1's complement $\rightarrow$

$$+x = +x$$

$$-x = +\bar{x}$$

eg. $+x = 0101 = x$

$$\bar{x} = 1010 = \bar{x}$$

highest val.

$$\bar{x} = \begin{array}{r} 111 \\ -0101 \leftarrow \text{given val} \\ \hline 1010 \end{array}$$

$\bar{x}$

let

$$x = +4 = 0100$$

$$\bar{x} = -4 = 1011$$

4 bit.

8 bit

6 bit

$$\begin{array}{r} 00000100 \\ \text{copy of} \uparrow \end{array}$$

$$000100$$

$$\begin{array}{r} 11111011 \\ \text{copy of} \uparrow \end{array}$$

6 bit.

$$111011$$

In 1's complement form,
signed magnitude
2's comp.

$$+ve \text{ no. } = \text{MSB} = 0$$

$$-ve \text{ no. } = \text{MSB} = 1.$$

Range of 1's Complement $\rightarrow$

for $n=3$ bit

$$-3 \text{ to } 3$$

$$= -3, -2, -1, -0, +0, +1, +2, +3.$$

for

n bit = same as signed mag. form.

$$-(2^{n-1} - 1) \text{ to } +(2^{n-1} - 1)$$

Calculation possible.

disadvantage $\rightarrow$

- Two diff. rep. of zero i.e. $+0$ & -0
- Extra addition if req. if carry is generated at time of addition operation.

(n-1)'s complement.

⑧ $(62)_{10} \xrightarrow[comp.]{9's} \begin{array}{r} 99 \\ - 62 \\ \hline 37 \end{array}$, ⑨ $(62)_8 \xrightarrow[comp.]{7's} \begin{array}{r} 77 \\ - 62 \\ \hline 15 \end{array}$

3). 2's complement form $\rightarrow$ (1's complement) $\rightarrow$ (byte)

$$+x = +x$$

$$-x = \overline{+x} + 1 = 1's \text{ comp.} + 1$$

$$+7 = 0111$$

$$+8 = 01000$$

} $\rightarrow$ same as signed and 1's complement

g.

$$-7 = \overline{+7} + 1 = \overline{0111} + 0001 = 1000 + 0001$$

$$\boxed{-7 \quad - \quad 1001}$$

Binary Number $\rightarrow$ (2's comp)	decimal no.
	+0
00	+1
01	
10	-2
11	-1

$$(11000)_{2's\ comp} = (?)_{10}$$

$\downarrow$
-ve

$$= -x = \overline{+x} + 1 = y$$

$$+x = +x = y$$

$$-x = \overline{+x} = y-1$$

$$x = \overline{y-1}$$

for $n = 2$ bit.

$$+ve = +0, +1$$

$$-ve = -1, -2$$

Range of number

$$-(2^{n-1}) \text{ to } (2^{n-1}-1)$$

$$n = 2 \text{ bit} = -2 \text{ to } +1$$

$$-2, -1, 0, +1$$

$$n = 4 \text{ bit} = -8 \text{ to } +7$$

$$y = 11000$$

$$y-1 = 11000 - 00001$$

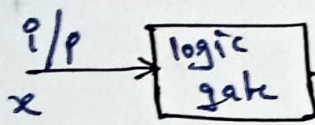
$$y-1 = 10111$$

$$x = \overline{y-1} = 01000$$

$$\boxed{-x = -8}$$

logic gates & Boolean Algebra →

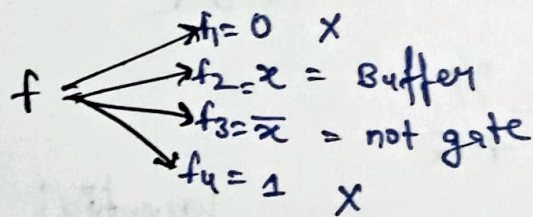
one input logic gate →



i/p x	o/p			
	f ₁	f ₂	f ₃	f ₄
0	0	0	1	1
1	0	1	0	1
	↓	↓	↓	↓
	0 NO	x choice	x choice	1 req.

four ckt possible.

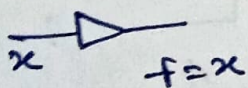
for n bit input 2^n or 2^{2^n} output possible.



1 input gate

Buffer

NOT gate



Truth table →

i/p	o/p
x	f
0	0
1	1

• Provide delay

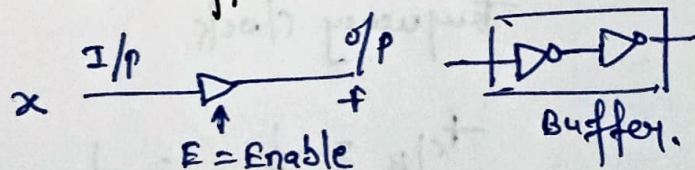
$\tau_{p.d.}$

• P.D. = Propagation

Delay.

• if multiple buffer are arranged then effective will be sum.

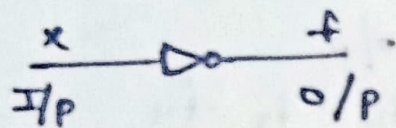
tristate buffer →



Enable	I/p	o/p
E	x	f
0	0	Hi-Z
0	1	Hi-Z
1	0	0
1	1	1

} 3 state

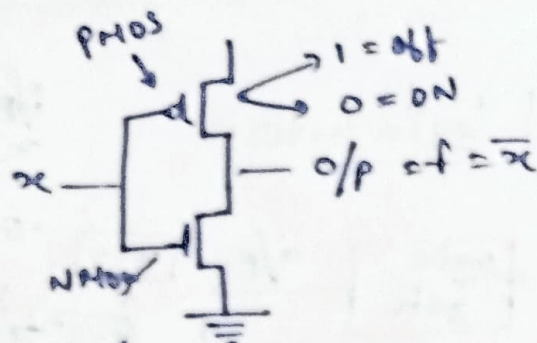
11. NOT gate: $\rightarrow$



Truth Table

x	$f = \bar{x}$
0	1
1	0

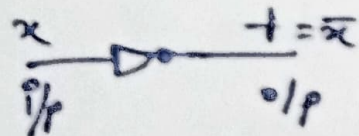
NOT gate by CMOS: $\rightarrow$



$x=0$ PMOS=ON
NMOS=OFF
 $f=1$
 $x=1$, PMOS=OFF
NMOS=ON
 $f=0$

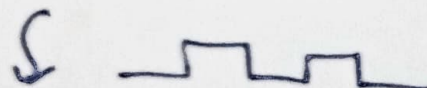
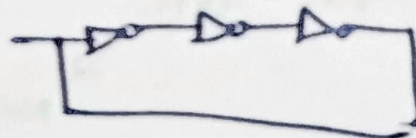
1 not gate = 1 PMOS + 1 NMOS
= 1 CMOS
= 2 nMOS

if odd No. of NOT gate connected in a code



$$\tau = n \cdot \tau_{pd}$$

sequential circuit

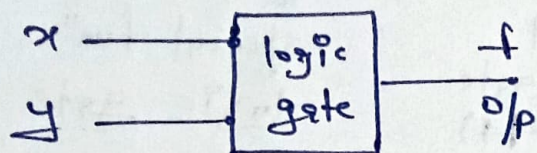


square wave

frequency clock

$$f_{clk} = \frac{1}{T_{clk}} = \frac{1}{2 \times n \times \tau_{pd}}$$

2 input logic gate



Boolean
functions
 2^{2^n}

$$= 16.$$

2 don't
step; logic
gate

10th logic
gate

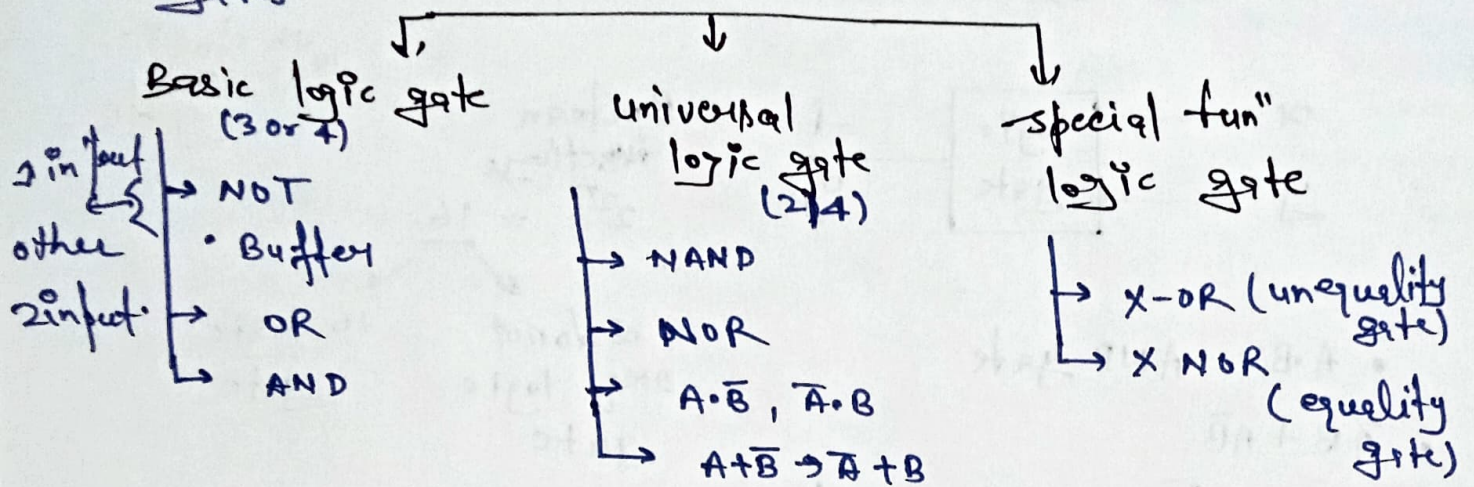
10 logic
gate

- $A \cdot B = \text{AND gate}$
- $\bar{A}B + A\bar{B}$
 $= A \oplus B = \text{X-OR gate}$
- $A + B = \text{OR gate}$
- $\overline{A \cdot B} = \overline{A + B} = \text{NOR gate}$
- $A \cdot B + \overline{A \cdot B}$
 $A \oplus B = \text{X-NOR gate}$
- $\bar{A} + \bar{B}$
 $\overline{A \cdot B} = \text{NAND gate}$

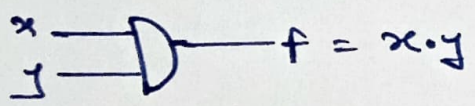
A	B	f_1	f_2	f_3	f_4	f_5	f_6	f_7	f_8	f_9	f_{10}	f_{11}	f_{12}	f_{13}	f_{14}	f_{15}	f_{16}
0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1
0	1	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1
1	0	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1
1	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1
		$\downarrow$ 0	$A \cdot B$	$A \cdot \bar{B}$	A	$\bar{A} \cdot B$	B	$\bar{A} + \bar{B}$ BA	$A + B$	$\bar{A}B + A\bar{B}$ $\bar{A} \cdot \bar{B}$	f_{10}	$\bar{B}$	$A + \bar{B}$	$\bar{A}$ $\bar{A} + B$	$A + B$	$\downarrow$ 1	

2 Input logic gates.

logic gate



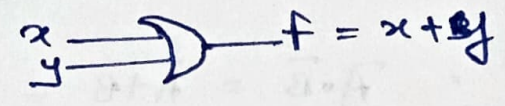
AND gate



x	y	f = x.y
0	0	0
0	1	0
1	0	0
1	1	1

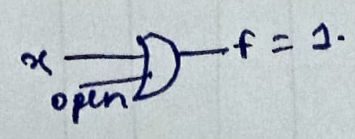
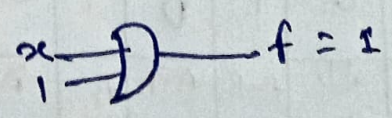
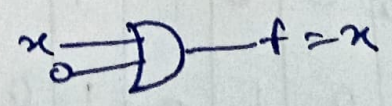
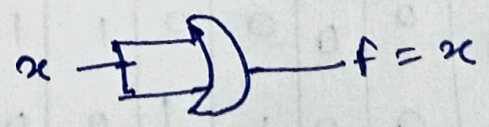
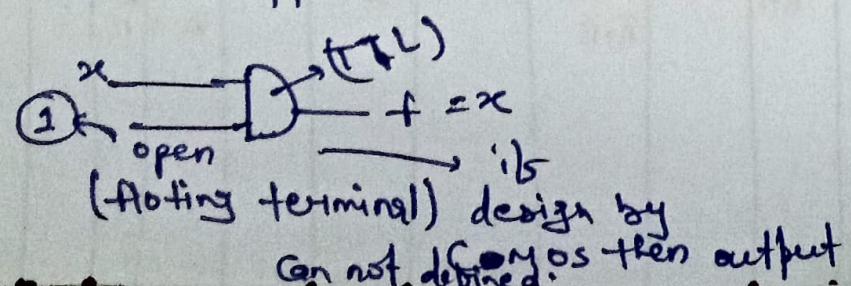
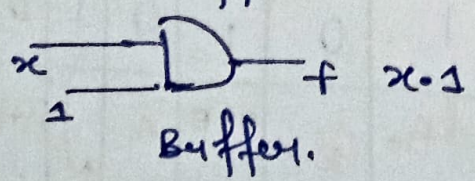
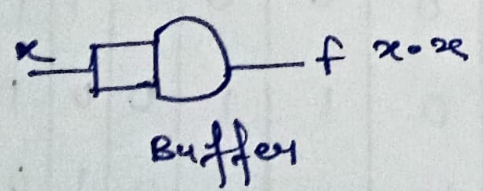
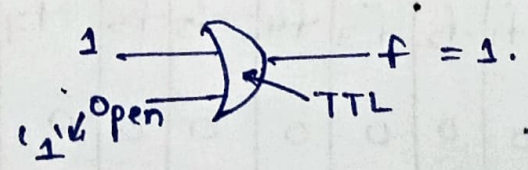
Majority 0/p = 0

OR gate



x	y	f = x+y
0	0	0
0	1	1
1	0	1
1	1	1

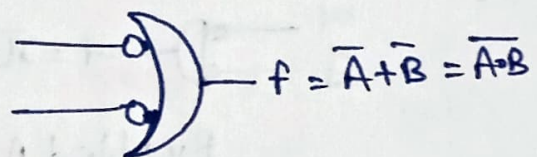
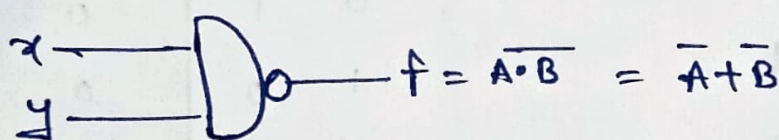
Majority 1/p = 1.



Universal logic gate

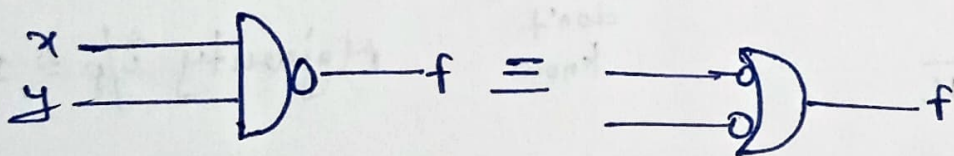
5.

* NAND gate $\rightarrow$
(AND + NOT)



Bubbled (NOT) + OR

Bubbled OR gate

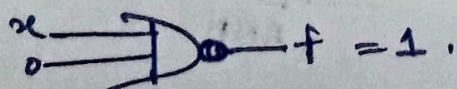
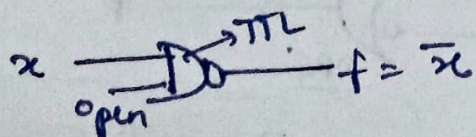
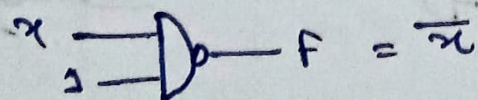
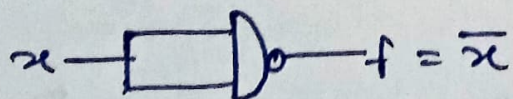


x	y	$f = \overline{x \cdot y} = \overline{x} + \overline{y}$
0	0	1
0	1	1
1	0	1
1	1	0

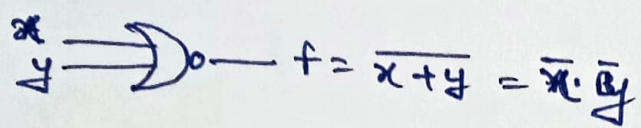
majority input = 0 = AND gate (G/30).

↓
o/p
↓
1.

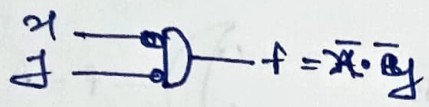
↓
here o/p
↓
0



2. NOR gate (OR + NOT) →

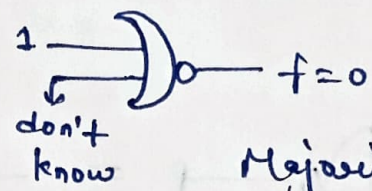
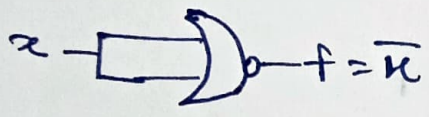


or

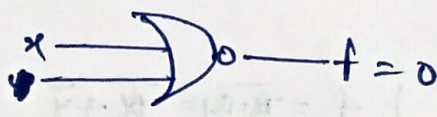
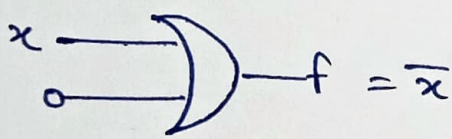


Bubbled AND

x	y	f = $\overline{x+y} = \overline{x} \cdot \overline{y}$
0	0	1
0	1	0
1	0	0
1	1	0

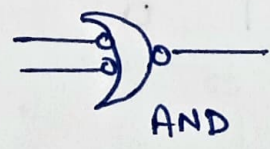
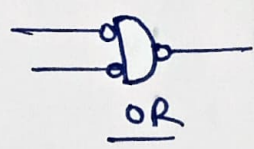


Majority i/p = 1.

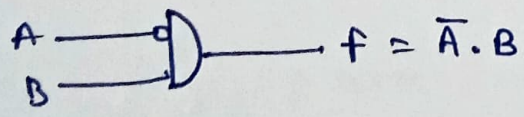


OR = NOR + NOT

AND = NAND + NOT



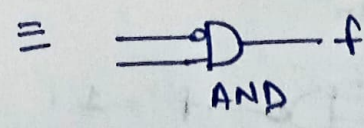
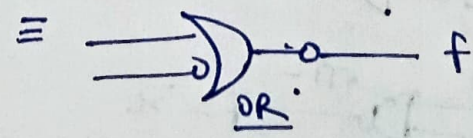
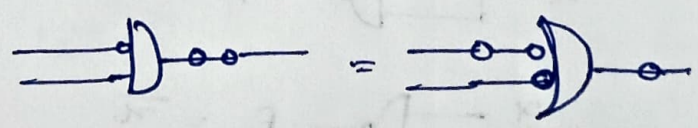
3. global 1 (A · B̄)



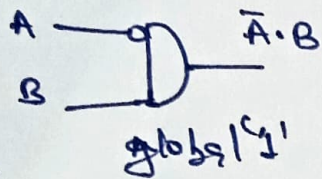
A	B	f = $\overline{A} \cdot B$
0	0	0
0	1	1
1	0	0
1	1	0

Majority i/p = No

Can not defined



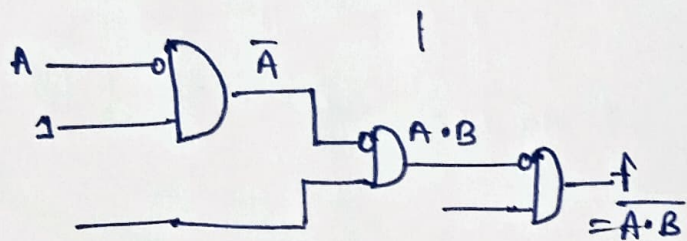
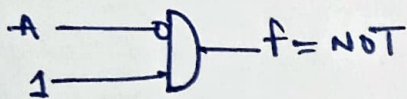
NAND gate by global '1' $\rightarrow$



$$NAND = \overline{A \cdot B} = \bar{A} + \bar{B}$$

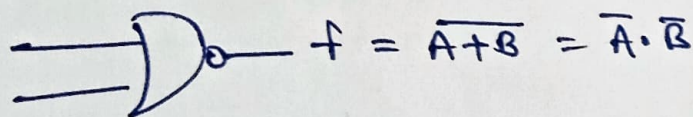


=

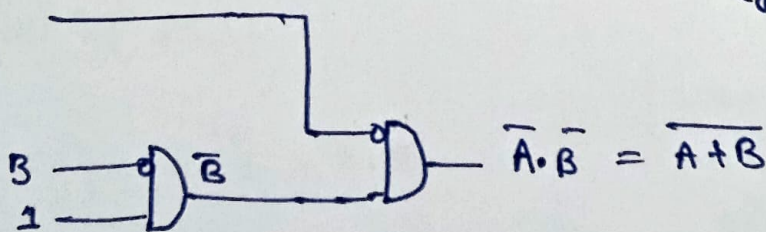


$$NAND = 3(\text{global '1'})$$

NOR gate by global '1' $\rightarrow$



$$NOR = 2(\text{global '1'})$$



special logic gates: $\rightarrow$

$$\begin{array}{c} \text{EX-OR} = \text{XOR} \\ \text{XNOR} \end{array} \Rightarrow f = A \oplus B$$

$$f = A \odot B$$

$$\begin{array}{c} \bar{A}B + A\bar{B} \\ \uparrow \\ A \oplus B \\ \downarrow \\ AB + \bar{A}\bar{B} \end{array}$$

(5*)

$$\text{XNOR} = \overline{\text{XOR}}$$

$$\text{XOR} = \overline{\text{XNOR}}$$

$$\begin{array}{l} \text{Buffer} = \overline{\text{NOT}} \\ \text{AND} = \overline{\text{NAND}} \\ \text{OR} = \overline{\text{NOR}} \end{array}$$

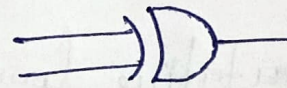
A	B	$A \oplus B$	$A \odot B$
0	0	0	1
0	1	1	0
1	0	1	0
1	1	0	1

if { odd 1 $\Rightarrow$ 1
even = 0. }

XOR

equality detector.

inequality detector



or

$$\boxed{+} \rightarrow f = A \oplus B$$

Boolean Algebra →

Boolean principle →

1. Demorgan's law → $\overline{\overline{A}} = A$, $\overline{\overline{x}} = x$

$$\overline{x \cdot y} = \overline{x} + \overline{y}$$

$$\overline{x + y} = \overline{x} \cdot \overline{y}$$

2. Idempotting law →

$$x + x = x \quad \left\{ \quad x \cdot x = x \right.$$

$$1 + 1 = 1 \quad \left\{ \quad 1 \cdot 1 = 1 \right.$$

$$0 + 0 = 0 \quad \left\{ \quad 0 \cdot 0 = 0 \right.$$

$$x(\text{NAND})x = \overline{x} \quad | \quad x(\text{NOR})x = \overline{x}$$

3. Commutative law →

$$x + y = y + x$$

$$x \cdot y = y \cdot x$$

$$\left\{ \begin{array}{l} x(\text{NAND})y = y(\text{NAND})x \\ x(\text{NOR})y = y(\text{NOR})x \end{array} \right.$$

4. Associative law →

$$(x + y) + z = x + (y + z)$$

$$(x \cdot y) \cdot z = x \cdot (y \cdot z)$$

$$\left\{ \begin{array}{l} \text{NAND \& NOR} \\ \text{do not follow associative} \\ \text{law.} \end{array} \right.$$

5. Compensation law →

$$x + \overline{x} = 1$$

$$x \cdot \overline{x} = 0$$

$$x(\text{NAND})\overline{x} = 1$$

$$x(\text{NOR})\overline{x} = 0$$

} NOT law
extra.

6. Distributive law $\rightarrow$

$$x(y+z) = xy + xz$$

$$x + yz = (x+y)(x+z)$$

7. Absorption law $\rightarrow$

$$x + x'y = (x+x')(x+y) = x+y$$

$$x + xy = (x+x')(x+y) = x(1+y) = x$$

8. Consensus law $\rightarrow$

$$xy + x'z + yz = xy + x'z$$

$$xy' + xz + yz = xy' + xz$$

9. Duality principle $\rightarrow$

+ve level logic $\begin{cases} 1 \rightarrow \text{high} \\ 0 \rightarrow \text{low} \end{cases}$

-ve level logic $\begin{cases} 1 \rightarrow \text{low} \\ 0 \rightarrow \text{high} \end{cases}$

AND $\xrightarrow{\text{Dual}}$ OR $\begin{cases} 0 \rightarrow 1 \\ 1 \rightarrow 0 \end{cases}$
 NAND $\xrightarrow{\text{Dual}}$ NOR

$$\left. \begin{aligned} f(x,y) &= \overline{x \cdot y} \\ f_D(x,y) &= \overline{x + y} \\ f'(x,y) &= x \cdot y \end{aligned} \right\} \begin{array}{l} \text{AND} \\ \text{OR} \\ \text{NOT only} \end{array}$$

$$\left. \begin{aligned} f(x,y) &= \overline{x + y} \\ f'(x,y) &= x + y \\ f_D(x,y) &= \overline{x \cdot y} \end{aligned} \right\} \begin{array}{l} \text{NOR} \\ \text{AND} \\ \text{NOT only} \end{array}$$

+ve level logic $\xrightarrow{\text{Dual}}$ -ve level logic $\left\{ \begin{array}{l} f'(x,y) = \overline{x + y} \\ f_D(x,y) = \overline{x \cdot y} \end{array} \right\}$

10. Complement of "fun"

let $f(x,y,z) = xy + yz + xz$

to complement in Boolean algr.

and to or
or to and
and complement
of each variable.

$$f'(x,y,z) = (\bar{x} + \bar{y}) \cdot (\bar{y} + \bar{z}) \cdot (\bar{x} + \bar{z})$$

Canonical form $\rightarrow$

Minterms $\rightarrow$ [standard product term]

x	y	minterms = 1
0	0	0 $\rightarrow x'y'$
1 $\rightarrow$ 0	1	1 $\rightarrow x'y$
2 $\leftarrow$ 1	0	1 $\rightarrow xy'$
3	1	0 $\rightarrow xy$

$$f(x,y) = \sum m(1,2) = \sum (1,2)$$

 $= x'y + xy'$

SOP = AND-OR ckt

SOP = NAND-NAND ckt

Maxterms: [standard sum term] $\rightarrow$

x	y	Maxterm = 0
0	0	0 $x+y \rightarrow 0$
0	1	1 $x+y' \rightarrow 1$
1	0	1 $x'+y \rightarrow 2$
1	1	1 $x'+y' \rightarrow 3$

$$f(x,y) = \prod M(0,3)$$

$$= (x+y)(x'+y')$$

POS $\rightarrow$ product of sum

POS = OR-AND ckt
POS = NOR-NOR ckt

Que.

$$f(x, y, z) = xy + yz + xz$$

write down sop & pos form of this boolean fun.

sol

$$\begin{aligned}
 f(x, y, z) &= xy(z+z') + (x+x')yz + x(y+y')z \\
 &= xyz + xyz' + x'yz + x'yz + x'yz + x'yz' \\
 &= \underset{\downarrow 7}{xyz} + \underset{\downarrow 6}{xyz'} + \underset{\downarrow 3}{x'yz} + \underset{\downarrow 5}{x'yz'}
 \end{aligned}$$

$$f(x, y, z) = \sum m(3, 5, 6, 7)$$

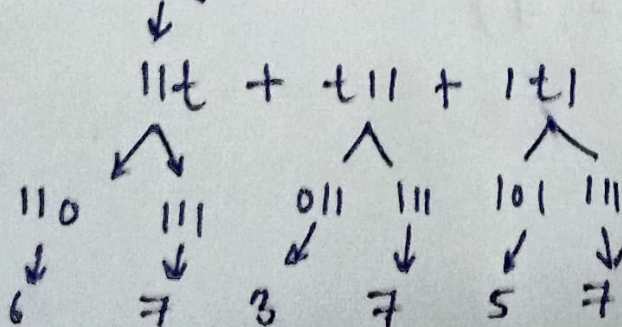
$$\pi M(0, 1, 2, 4)$$

$$f'(x, y, z) = \sum m(0, 1, 2, 4)$$

$$\pi M(3, 5, 6, 7)$$

another simple way $\rightarrow$

$$f(x, y, z) = xy + yz + xz$$



$$\Rightarrow f(x, y, z) = \sum m(3, 5, 6, 7)$$

Que. $f(x, y, z) = (x+z')(y'+z')(x'+y)$ Ans. for Canonical form

Ans

$$\begin{aligned} f(x, y, z) &= (x+y \cdot y' + z') (x \cdot x' + y' + z') + (x' + y + z z') \\ &= \underbrace{(x+y+z')}_{001} \underbrace{(x+y'+z')}_{011} + \underbrace{(x+y'+z')}_{011} \underbrace{(x'+y'+z')}_{111} \\ &\quad + \underbrace{(x'+y+z)}_{100} \underbrace{(x'+y+z')}_{101} \end{aligned}$$

$$\pi_m (1, 3, 4, 5, 7)$$

$$\sum_m (0, 2, 6)$$

Note this is Maxterm

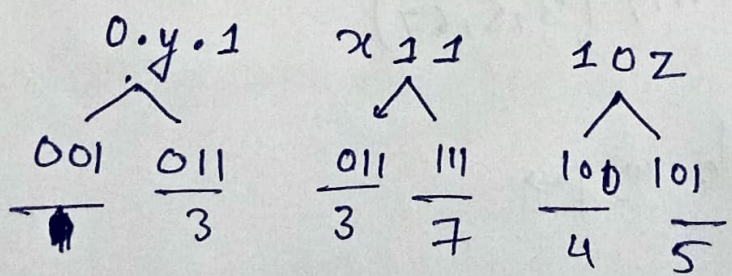
$$\begin{aligned} x &\rightarrow 0 \\ x' &\rightarrow 1 \end{aligned}$$

but in min term

$$\begin{aligned} x &\rightarrow 1 \\ x' &\rightarrow 0 \end{aligned}$$

another simple way $\rightarrow$

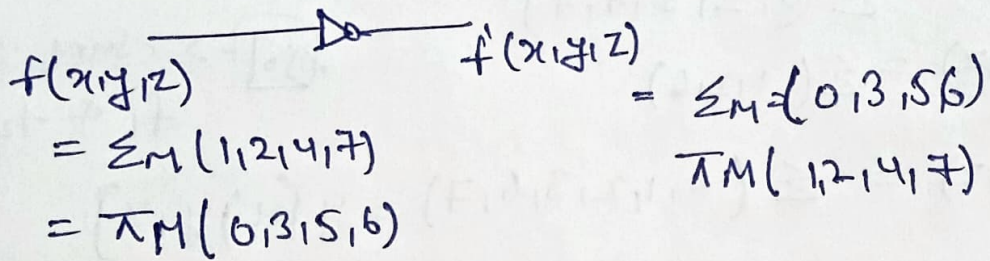
$$f(x, y, z) = (x+z') (y'+z') (x'+y)$$



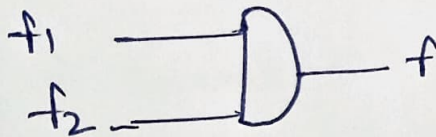
$$\pi_m (1, 3, 4, 5, 7)$$

• How to process any boolean funⁿ from logic gates: →

→ NOT gate →



→ AND gate →



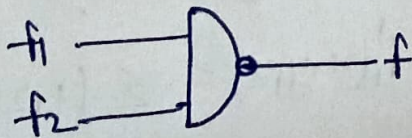
$f_1(x,y,z) = \sum(1,2,3,4,7)$ $f(x,y,z) = ?$
 $f_2(x,y,z) = \sum(0,1,4,6)$

ex common term will be answer.

$$f(x,y,z) = \sum(1,4) = \pi(0,2,3,5,6,7) = \prod(x,y,z)$$

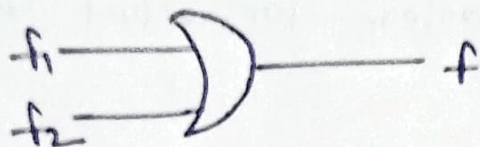
NOT POS (πM) से common नहीं लेना है।

→ NAND gate →



$f_1(x,y,z) = \sum(1,2,3,4,7)$ $\Rightarrow \prod(x,y,z) = \sum(1,4)$
 $f_2(x,y,z) = \sum(0,1,4,6)$ $f(x,y,z) = \pi(1,4)$
 $= \sum(0,2,3,5,6,7)$

OR gate →



$$f_1(x, y, z) = \sum (0, 2, 3, 6, 7)$$

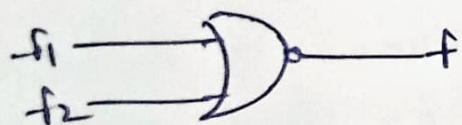
$$f_2(x, y, z) = \sum (1, 2, 6)$$

006 → sum of both f_1 & f_2 .

$$f(x, y, z) = \sum (0, 1, 2, 3, 6, 7) = g(x, y, z)$$

NOTE MAXTERM (π M) में add नहीं करना

NOR gate →



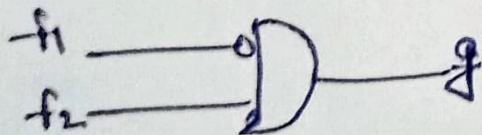
$$f_1(x, y, z) = \sum (0, 2, 3, 6, 7)$$

$$f_2(x, y, z) = \sum (1, 2, 6)$$

$$g(x, y, z) = \sum (0, 1, 2, 3, 6, 7)$$

$$f(x, y, z) = \sum (4, 5) = \pi (0, 1, 2, 3, 6, 7)$$

Global 1



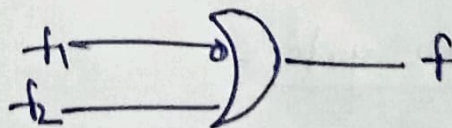
$$f_1(x, y, z) = \sum (0, 3, 5, 6)$$

$$f_2(x, y, z) = \sum (0, 1, 2, 6)$$

$$g(x, y, z) = \sum (1, 2)$$

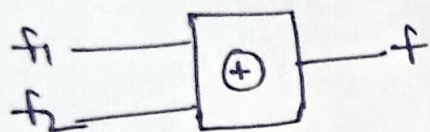
$$= \pi (0, 3, 4, 5, 6, 7)$$

Global 2

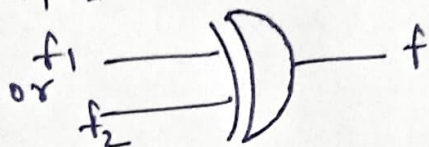


$$f_1(x, y, z) = \sum (1, 2, 4, 7)$$

$$f(x, y, z) = \sum (0, 1, 2, 4, 6, 7)$$

X-OR gate

$$f_1 \bar{f}_2 + \bar{f}_1 f_2$$



$$f_1(x, y, z) = \sum (0, 1, 6, 7)$$

$$f_1'(x, y, z) = \sum (2, 3, 4, 5)$$

$$f_2(x, y, z) = \sum (0, 1, 2, 3, 4, 5)$$

$$f_2'(x, y, z) = \sum (6, 7)$$

$$f(x, y, z) = \sum (6, 7) + \sum (2, 3, 4, 5)$$

$$= \sum (2, 3, 4, 5, 6, 7) = \pi(0, 1)$$

Sol जो दोनों में common है और जो नहीं है उसे छोड़ दो।
But this is the solⁿ for XNOR